

Unit 7 Worksheet 1

$$1. \cos^3\theta + \sin^2\theta \csc\theta = \cos\theta$$

$$\csc\theta(\cos^2\theta + \sin^2\theta) =$$

$$\csc\theta(1) =$$

$$\csc\theta = \sqrt{\quad}$$

$$6. \frac{\cot\theta}{\csc\theta+1} = \tan\theta$$

$$\csc\theta+1 =$$

$$\frac{\cot\theta}{\cot^2\theta} =$$

$$\frac{1}{\cot\theta} =$$

$$2. \csc^2\theta - \cos^2\theta \csc^2\theta = 1$$

$$\csc^2\theta(1 - \cos^2\theta) =$$

$$\csc^2\theta (\sin^2\theta) =$$

$$\frac{1}{\sin^2\theta} (\sin^2\theta) =$$

$$1 =$$

$$7. \sec\theta \sin\theta \csc\theta = 1$$

$$\frac{1}{\cos\theta} \sin\theta \frac{\cos\theta}{\sin\theta} =$$

$$1 = 1$$

$$3. \sec\theta \sin\theta = \tan\theta$$

$$\frac{1}{\cos\theta} \cdot \sin\theta =$$

$$\frac{\sin\theta}{\cos\theta} =$$

$$\tan\theta = \tan\theta$$

$$8. \cot\theta \csc\theta \tan^2\theta = \sec\theta$$

$$\frac{\cos\theta}{\sin\theta} \cdot \frac{1}{\sin\theta} \cdot \frac{\sin\theta}{\cos\theta} =$$

$$\frac{1}{\cos\theta} =$$

$$\sec\theta = \sec\theta$$

$$4. \frac{\csc\theta}{\sec\theta} = \cot\theta$$

$$\frac{1}{\sin\theta} =$$

$$\frac{1}{\sin\theta} \cdot \cos\theta =$$

$$\frac{\cos\theta}{\sin\theta} =$$

$$\cot\theta = \cot\theta$$

$$9. \cos^2\theta - \sin^2\theta = 2\cos^2\theta - 1$$

$$\cos^2\theta - (1 - \cos^2\theta) =$$

$$\cos^2\theta - 1 + \cos^2\theta =$$

$$2\cos^2\theta - 1 = 2\cos^2\theta - 1$$

$$5. \frac{\sec^2\theta - 1}{\tan\theta} = \tan\theta$$

$$\tan\theta$$

$$\frac{\tan^2\theta}{\tan\theta} =$$

$$\tan\theta = \tan\theta$$

$$10. \cos^2\theta - \sin^2\theta = 1 - 2\sin^2\theta$$

$$(1 - \sin^2\theta) - \sin^2\theta =$$

$$1 - 2\sin^2\theta = 1 - 2\sin^2\theta$$

$$11. \cot\theta \sin\theta = \cos\theta$$

$$\frac{\cos\theta}{\sin\theta} \cdot \sin\theta =$$

$$\cos\theta = \cos\theta$$

$$\frac{\sin\theta \cdot \cos\theta}{\cos\theta}$$

$$\frac{\tan\theta}{\sec\theta} = \sin\theta$$

$$\frac{\sin\theta \cdot \cos\theta}{\cos\theta} =$$

$$\sin\theta = \sin\theta$$

$$13. \sin\theta (1 + \csc\theta) = \sin\theta + 1$$

$$\sin\theta + \sin\theta \csc\theta =$$

$$\sin\theta + \sin\theta \cdot \frac{1}{\sin\theta} =$$

$$\sin\theta + 1 = \sin\theta + 1$$

$$14. (1 + \tan\theta)^2 = \sec^2\theta + 2\tan\theta$$

$$1 + 2\tan\theta + \tan^2\theta =$$

$$(1 + \tan^2\theta) + 2\tan\theta =$$

$$\sec^2\theta + 2\tan\theta = \sec^2\theta + 2\tan\theta$$

$$15. (1 + \tan^2\theta) \cos^2\theta = 1$$

$$\cos^2\theta + \tan^2\theta \cos^2\theta =$$

$$\cos^2\theta + \frac{\sin^2\theta}{\cos^2\theta} \cos^2\theta =$$

$$\cos^2\theta + \sin^2\theta =$$

$$1 = 1$$

$$16. \csc\theta = \sec\theta - \sin\theta \tan\theta$$

$$\sec\theta - \sin\theta \cdot \frac{\sin\theta}{\cos\theta}$$

$$\sec\theta - \frac{\sin^2\theta}{\cos\theta}$$

$$= \frac{1}{\cos\theta} - \frac{\sin^2\theta}{\cos\theta}$$

$$= \frac{1 - \sin^2\theta}{\cos\theta}$$

$$= \frac{\cos^2\theta}{\cos\theta}$$

$$\cos\theta \cdot \cos\theta$$

$$17. (\sec\theta + \tan\theta)(\sec\theta - \tan\theta) = 1$$

$$\sec^2\theta - \tan^2\theta =$$

$$\frac{1}{\cos^2\theta} - \frac{\sin^2\theta}{\cos^2\theta} =$$

$$\frac{1 - \sin^2\theta}{\cos^2\theta} =$$

$$\frac{\cos^2\theta}{\cos^2\theta} =$$

$$1 = 1$$

$$18. \frac{\sec\theta}{\csc^2\theta} = \sec\theta - \cos\theta$$

$$= \frac{1}{\cos\theta} - \cos\theta$$

$$= \frac{1}{\cos\theta} - \frac{\cos^2\theta}{\cos\theta}$$

$$= \frac{1 - \cos^2\theta}{\cos\theta}$$

$$= \frac{\sin^2\theta}{\cos\theta}$$

$$= \frac{1}{\csc\theta} \cdot \sec\theta$$

$$19. \frac{\sec\theta}{\csc^2\theta} = \sec\theta - \csc\theta$$

$$\frac{1 - 2\csc\theta}{\csc\theta} = \tan\theta - 2\sec\theta$$

$$\frac{1}{\csc\theta} - \frac{2\csc\theta}{\csc\theta} =$$

$$\tan\theta - \frac{2\csc\theta}{\csc\theta \cdot \sin\theta} =$$

$$\tan\theta - \frac{2}{\cos\theta} =$$

$$\tan\theta - 2\sec\theta = \tan\theta - 2\sec\theta$$

$$20. \frac{\sec^2 \theta - 1}{\tan \theta} = \tan \theta$$

$$\frac{\tan^2 \theta}{\tan \theta} =$$
$$\tan \theta = \tan \theta$$

$$21. \sin\theta + \cos\theta \cot\theta = \csc\theta$$

$$\begin{aligned} \sin\theta + \cos\theta \frac{\cos\theta}{\sin\theta} &= \\ \left(\frac{\sin\theta}{\sin\theta}\right) \sin\theta + \frac{\cos^2\theta}{\sin\theta} &= \\ \frac{\sin^2\theta}{\sin\theta} + \frac{\cos^2\theta}{\sin\theta} &= \\ \frac{\sin^2\theta + \cos^2\theta}{\sin\theta} &= \\ \frac{1}{\sin\theta} &= \\ \csc\theta &= \csc\theta \end{aligned}$$

$$22. \cos\theta (\csc\theta - \sec\theta) = \cot\theta - 1$$

$$\begin{aligned} \cos\theta \csc\theta - \cos\theta \sec\theta &= \\ \cos\theta \frac{1}{\sin\theta} - \cos\theta \frac{1}{\cos\theta} &= \\ \cos\theta - 1 &= \cot\theta - 1 \end{aligned}$$

$$23. \frac{\cos\theta}{1-\sin^2\theta} = \sec\theta$$

$$\begin{aligned} \frac{\cos\theta}{\cos^2\theta} &= \\ \frac{1}{\cos\theta} &= \\ \sec\theta &= \sec\theta \end{aligned}$$

$$24. \tan^2\theta - \tan^2\theta \sin^2\theta = \sin^2\theta$$

$$\tan^2\theta (1 - \sin^2\theta) =$$

$$\tan^2\theta \cdot \cos^2\theta =$$

$$\frac{\sin^2\theta}{\cos^2\theta} \cdot \cos^2\theta =$$

$$\sin^2\theta = \sin^2\theta$$

25. $\frac{\cot\theta}{1+\cot^2\theta} = \sin\theta \cos\theta$

$$\frac{\cot\theta}{\csc^2\theta} =$$

$$\frac{\cos\theta}{\sin\theta} \cdot \frac{\sin^2\theta}{\sin\theta} =$$

$$\cos\theta \sin\theta =$$

$$\sin\theta \cos\theta = \sin\theta \cos\theta$$

26. $\frac{1+\tan^2\theta}{\cos^2\theta} = \sec^4\theta$

$$\frac{\sec^2\theta}{\cos^2\theta} =$$

$$\frac{1}{\cos^2\theta}$$

$$\sec^2\theta \cdot \sec^2\theta =$$

$$\sec^4\theta = \sec^4\theta$$

27. $\frac{\sin\theta + \cos\theta}{\sin\theta \cos\theta} = \sec\theta + \csc\theta$

$$\frac{\sin\theta}{\sin\theta \cos\theta} + \frac{\cos\theta}{\sin\theta \cos\theta} =$$

$$\frac{1}{\cos\theta} + \frac{1}{\sin\theta} =$$

$$\sec\theta + \csc\theta = \sec\theta + \csc\theta$$

$$28. \frac{\sec \theta + \tan \theta}{\csc \theta + \cot \theta} = \sin \theta \sec^2 \theta$$

$$\frac{\frac{1}{\cos \theta} + \frac{\sin \theta}{\cos \theta}}{\frac{1}{\sin \theta} + \frac{\cos \theta}{\sin \theta}}$$

$$\frac{1 + \sin \theta}{\cos \theta} \cdot \frac{\sin \theta}{\cos \theta \sin \theta + \cos \theta}$$

$$\frac{(1 + \sin \theta) \cdot \sin \theta}{\cos \theta \cdot (\cos \theta \sin \theta + \cos \theta)} =$$

$$\frac{\sin \theta (1 + \sin \theta)}{\cos \theta (\sin \theta + 1)} =$$

$$\frac{\sin \theta}{\cos^2 \theta} =$$

$$\sin \theta \sec^2 \theta = \sin \theta \sec^2 \theta$$

$$29. \frac{(1 + \sin \theta)^2}{\cos^2 \theta} = \frac{1 + \sin \theta}{1 - \sin \theta}$$

$$\frac{(1 + \sin \theta)^2}{1 - \sin^2 \theta} =$$

$$\frac{(1 + \sin \theta)^2}{(1 + \sin \theta)(1 - \sin \theta)} =$$

$$\frac{1 + \sin \theta}{1 - \sin \theta} = \frac{1 + \sin \theta}{1 - \sin \theta}$$

30.

$$\frac{1 + \sec \theta}{\tan \theta + \sin \theta} = \csc \theta$$

$$\begin{aligned} \frac{1 + \frac{1}{\cos \theta}}{\frac{\sin \theta}{\cos \theta} + \sin \theta} &= \\ \frac{\frac{\cos \theta + 1}{\cos \theta}}{\frac{\sin \theta + \sin \theta - \cos \theta}{\cos \theta}} &= \end{aligned}$$

$$\frac{\cos \theta + 1}{\cos \theta} \cdot \frac{\cos \theta}{\sin \theta + \sin \theta - \cos \theta} =$$

$$\frac{\cos \theta + 1}{\sin \theta + \sin \theta \cos \theta} =$$

$$\frac{(\cos \theta + 1)}{\sin \theta(1 + \cos \theta)} =$$

$$\frac{1}{\sin \theta} =$$

$$\csc \theta = \csc \theta$$

$$\begin{aligned}
 31. \quad & \csc\theta \cos^2\theta + \sin\theta = \csc\theta \\
 & \csc\theta \cos^2\theta + \sin\theta \cdot \frac{\csc\theta}{\csc\theta} = \\
 & \csc\theta (\cos^2\theta + \sin\theta \cdot \frac{1}{\csc\theta}) = \\
 & \csc\theta (\cos^2\theta + \sin\theta \cdot \sin\theta) = \\
 & \csc\theta (\cos^2\theta + \sin^2\theta) = \\
 & \csc\theta (1) = \\
 & \csc\theta = \csc\theta
 \end{aligned}$$

$$\begin{aligned}
 32. \quad & \frac{\csc^2\theta}{\csc^2\theta - 1} = \sec^2\theta \\
 & \frac{\csc^2\theta}{\csc^2\theta - 1} = \\
 & \frac{\csc^2\theta}{\cot^2\theta} = \\
 & \frac{1}{\sin^2\theta} \cdot \frac{\sin^2\theta}{\cos^2\theta} = \\
 & \frac{1}{\cos^2\theta} = \\
 & \sec^2\theta = \sec^2\theta
 \end{aligned}$$

$$\begin{aligned}
 33. \quad & \sin\theta \left(\frac{\cot\theta}{\sec\theta} + \csc\theta \right) = \cos^2\theta + 1 \\
 & \sin\theta \left(\frac{\cos\theta}{\sin\theta} \cdot \cos\theta + \frac{1}{\sin\theta} \right) = \\
 & \sin\theta \left(\frac{\cos^2\theta}{\sin\theta} + \frac{1}{\sin\theta} \right) = \\
 & \cos^2\theta + 1 = \cos^2\theta + 1
 \end{aligned}$$

$$\begin{aligned}
 34. \frac{2\cos^2\theta - \sin^2\theta + 1}{\cos\theta} &= 3\cos\theta \\
 \frac{2\cos^2\theta + (\sin^2\theta + 1)}{\cos\theta} &= \\
 \frac{2\cos^2\theta + \cos^2\theta}{\cos\theta} &= \\
 \frac{3\cos^2\theta}{\cos\theta} &= \\
 3\cos\theta &= 3\cos\theta
 \end{aligned}$$

$$\begin{aligned}
 35. \csc\theta - \sin\theta &= \cot\theta \cos\theta \\
 \frac{1}{\sin\theta} - \sin\theta &= \\
 \frac{1}{\sin\theta} - \frac{\sin^2\theta}{\sin\theta} &= \\
 \frac{1 - \sin^2\theta}{\sin\theta} &= \\
 \frac{\cos^2\theta}{\sin\theta} &= \\
 \frac{\cos\theta}{\sin\theta} \cdot \cos\theta &= \\
 \cot\theta \cdot \cos\theta &= \cot\theta \cos\theta
 \end{aligned}$$

$$\begin{aligned}
 36. \frac{1}{1-\cos\theta} + \frac{1}{1+\cos\theta} &= 2\csc^2\theta \\
 \frac{1-\cos\theta + 1+\cos\theta}{(1-\cos\theta)(1+\cos\theta)} &= \\
 \frac{2}{1-\cos^2\theta} &= \\
 \frac{2}{\sin^2\theta} &= \\
 2\csc^2\theta &= 2\csc^2\theta
 \end{aligned}$$

$$37. \frac{1 + \tan \theta}{\tan \theta} = 1 + \cot \theta$$

$$\frac{1}{\tan \theta} + \frac{\tan \theta}{\tan \theta} =$$

$$\cot \theta + 1 =$$

$$1 + \cot \theta = 1 + \cot \theta$$

$$38. \frac{\cos \theta + \tan \theta}{\sin \theta} = \sec \theta + \cot \theta$$

$$\frac{\cos \theta}{\sin \theta} + \frac{\tan \theta}{\sin \theta} =$$

$$\cot \theta + \frac{\sin \theta}{\sin \theta \cos \theta} =$$

$$\cot \theta + \frac{1}{\cos \theta} =$$

$$\cot \theta + \sec \theta =$$

$$\sec \theta + \cot \theta = \sec \theta + \cot \theta$$

$$39. \csc^4 \theta - \cot^4 \theta = 2 \csc^2 \theta - 1$$

$$\frac{1}{\sin^4 \theta} - \frac{\cos^4 \theta}{\sin^4 \theta} = \frac{2}{\sin^2 \theta} - 1$$

$$\frac{1 - \cos^4 \theta}{\sin^4 \theta} = \frac{2}{\sin^2 \theta} - \frac{2 \sin^2 \theta}{\sin^2 \theta}$$

$$\frac{(1 - \cos^2 \theta)(1 + \cos^2 \theta)}{\sin^2 \theta} = \frac{2 - \sin^2 \theta}{\sin^2 \theta}$$

$$\frac{(1 - \cos^2 \theta)(1 + \cos^2 \theta)}{(1 - \cos^2 \theta)(1 + \cos^2 \theta)} = \frac{1}{\sin^2 \theta} + \cot^2 \theta$$

$$\frac{1 + \cos^2 \theta}{1 - \cos^2 \theta}$$

$$\frac{1 - \cos^2 \theta}{\sin^2 \theta}$$

$$\csc^2 \theta + (-\csc^2 \theta - 1)$$

$$\csc^2 \theta + (\csc^2 \theta - 1) =$$

$$2 \csc^2 \theta - 1 = \checkmark$$

$$40. \frac{\cos\theta + \cot\theta}{\csc\theta + 1} = \cos\theta$$

$$\frac{\cos\theta + \frac{\cos\theta}{\sin\theta}}{\frac{1}{\sin\theta} + 1}$$

$$\frac{\sin\theta\cos\theta + \cos^2\theta}{\sin\theta}$$

$$\frac{\sin\theta}{\frac{1}{\sin\theta} + \frac{\sin\theta}{\sin\theta}} =$$

$$\frac{\sin\theta\cos\theta + \cos^2\theta}{\sin\theta}$$

$$\frac{\sin\theta}{1 - \frac{\sin\theta}{\sin\theta}} =$$

$$\frac{\sin\theta\cos\theta + \cos^2\theta}{\sin\theta} \cdot \frac{\sin\theta}{1 - \frac{\sin\theta}{\sin\theta}} =$$

$$\cos\theta(\sin\theta + 1) =$$

$$(1 + \sin\theta)$$

$$\cos\theta = \cos\theta$$

$$41. \frac{1 + \sec \theta}{\tan \theta + \sin \theta} = \csc \theta$$

$$\begin{aligned} & \frac{1 + \frac{1}{\cos \theta}}{\frac{\sin \theta}{\cos \theta} + \frac{\sin \theta \cdot \cos \theta}{\cos \theta}} = \\ & \frac{\cos \theta + 1}{\cos \theta} = \\ & \frac{\cos \theta}{\sin \theta (1 + \cos \theta)} = \\ & \frac{\cos \theta}{\cos \theta + 1} \cdot \frac{\cos \theta}{\sin \theta (1 + \cos \theta)} = \\ & \frac{1}{\sin \theta} = \\ & \csc \theta = \csc \theta \end{aligned}$$

$$\begin{aligned} 42. \frac{2 - \sec^2 \theta}{\sec \theta} &= \frac{1 - 2 \sin^2 \theta}{\cos \theta} \\ &= \frac{1 - 2(1 - \cos^2 \theta)}{\cos \theta} \\ &= \frac{1 - 2 + 2 \cos^2 \theta}{\cos \theta} \\ &= \frac{-1 + 2 \cos^2 \theta}{\cos \theta} \\ &= \frac{-1}{\cos \theta} + \frac{2 \cos^2 \theta}{\cos \theta} \\ &= -\sec \theta + 2 \cos \theta \\ &= -\sec \theta + \frac{2}{\sec \theta} \\ &= -\frac{\sec^2 \theta}{\sec \theta} + \frac{2}{\sec \theta} \\ &= \frac{2 - \sec^2 \theta}{\sec \theta} \end{aligned}$$

$$42. \frac{1}{\sec\theta - \tan\theta} = \sec\theta + \tan\theta$$

$$\frac{\frac{1}{\cos\theta} - \frac{\sin\theta}{\cos\theta}}{\frac{1-\sin\theta}{\cos\theta}} =$$

$$\frac{\cos\theta}{1-\sin\theta} =$$

$$\frac{\cos\theta(1+\sin\theta)}{(1-\sin\theta)(1+\sin\theta)} =$$

$$\frac{\cos\theta + \cos\theta\sin\theta}{1-\sin^2\theta} =$$

$$\frac{\cos\theta + \cos\theta\sin\theta}{\cos^2\theta} =$$

$$\frac{\cos\theta + \cos\theta\sin\theta}{\cos^2\theta} =$$

$$\frac{1 + \frac{\sin\theta}{\cos\theta}}{\cos\theta} =$$

$$\sec\theta + \tan\theta = \sec\theta + \tan\theta$$

$$44. 1 + \cos\theta = \cot\theta (\sin\theta + \tan\theta)$$

$$\begin{aligned} &= \cot\theta \sin\theta + \cot\theta + \cot\theta \\ &= \frac{\cos\theta}{\sin\theta} \sin\theta + 1 \\ &= \cos\theta + 1 \end{aligned}$$

$$45. 1 - \sin\theta = \tan\theta (\cot\theta - \cos\theta)$$

$$\begin{aligned} &= \tan\theta \cot\theta - \tan\theta \cos\theta \\ &= 1 - \frac{\sin\theta}{\cos\theta} \cdot \cos\theta \\ &= 1 - \sin\theta \end{aligned}$$

$$46. \frac{\tan\theta}{1 + \tan^2\theta} = \sin\theta \cos\theta$$

$$\frac{\tan\theta}{\sec^2\theta} =$$

$$\frac{\sin\theta}{\cos\theta} =$$

$$\frac{\sin\theta}{\cos\theta \sec^2\theta} =$$

$$\frac{\sin\theta}{\sec\theta} =$$

$$\sin\theta \cdot \cos\theta = \sin\theta \cos\theta$$

$$47. \frac{(\sec\theta - \tan\theta)^2}{\frac{1 - \sin\theta}{\cos^2\theta}} = \frac{1 - \sin\theta}{1 + \sin\theta}$$

$$\begin{aligned} &= \frac{(\sec\theta - \tan\theta)^2}{\frac{(1 - \sin\theta)^2}{\cos^2\theta}} \\ &= \frac{(1 - \sin\theta)^2}{(1 + \sin\theta)(1 - \sin\theta)} \end{aligned}$$

$$\rightarrow \frac{(1 - \sin\theta)^2}{1 - \sin^2\theta} =$$

$$\frac{(1 - \sin\theta)^2}{(1 + \sin\theta)(1 - \sin\theta)} =$$

$$\frac{1 - \sin\theta}{1 + \sin\theta} = \frac{1 - \sin\theta}{1 + \sin\theta}$$

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48.
$$\frac{1-\cos\theta}{1+\cos\theta} = \frac{\cos\theta}{\sin\theta}$$

$$\frac{(1-\cos\theta)(1-\cos\theta)}{(1+\cos\theta)(1-\cos\theta)} =$$
$$\frac{(1-\cos\theta)^2}{1-\cos^2\theta} =$$
$$\frac{(1-\cos\theta)^2}{\sin^2\theta} =$$
$$\frac{1-\cos\theta}{\sin\theta} =$$

49.
$$\frac{\sec\theta + \tan\theta}{\sec\theta - \tan\theta} = \frac{1+\sin\theta}{\cos\theta}$$

$$\frac{\frac{1}{\cos\theta} + \frac{\sin\theta}{\cos\theta}}{\frac{1}{\cos\theta} - \frac{\sin\theta}{\cos\theta}} =$$

$$\frac{\frac{1+\sin\theta}{\cos\theta}}{\frac{1-\sin\theta}{\cos\theta}} =$$

$$\frac{1+\sin\theta}{\cos\theta}, \frac{\cos\theta}{1-\sin\theta} =$$

$$\sqrt{\frac{(1+\sin\theta)^2}{\cos^2\theta}} =$$

$$\frac{1+\sin\theta}{\cos\theta} = \frac{1+\sin\theta}{\cos\theta}$$

$$\frac{1+\sin\theta}{1-\sin\theta}, \frac{(1+\sin\theta)}{(1+\sin\theta)} =$$

$$\sqrt{\frac{(1+\sin\theta)^2}{1-\sin^2\theta}}$$